# ALGEBRA Chapter 3: Algebra 

## Part 11: Solving Linear Equations

Starter (with the unknown on both sides)
Video
Worksheet - I'm giving it a try!
Worksheet - I'm building my confidence! Worksheet - I'm ready for anything!
Extension

Answer 4 questions to make a straight line vertically, horizontally or diagonally.

| Write 42 as a product of prime factors | $\begin{aligned} & \text { If } a=1, b=2 \\ & \text { and } c=-5, \\ & \text { calculate } \\ & 4 a+b c \end{aligned}$ | A table that used to cost $£ 180$ has decreased in price by $61 \%$. How much does it cost now? | The ratio of red to blue sweets is $1: 3$ and blue to green sweets is $1: 5$. What is the ratio of red to green sweets? |
| :---: | :---: | :---: | :---: |
| $154^{\circ}$ | Factorise$4 a^{2}-10 a b$ | Find the $n$th term of the sequence 6,10,14,18,22 | Calculate$2 / 4 \times 1 / 7$ |
|  |  |  |  |
| $\bigcirc$ Calculate $e^{\text {e }}$ |  |  |  |
| Calculate $1 / 8+3 / 5$ | $\begin{aligned} & \text { Estimate } \\ & 14.96 \times 3.76 \end{aligned}$ | Share 36 in the ratio 9:3 | Expand and simplify $(x-9)(x+4)$ |
| Solve $7(7 y+1)=-91$ | The mean of these 4 numbers is 7.5 . Calculate the missing value. 3,3,13,? | Does the coordinate $(2,8)$ lie on the graph $y=3 x-1$ ? | Calculate the size of one interior angle in a regular heptagon. |


| $2 \times 3 \times 7$ | -6 | $£ 70.20$ | $1: 15$ |
| :---: | :---: | :---: | :---: |
| $26^{\circ}$ | $2 a(2 a-5 b)$ | $4 n+2$ | $1 / 14$ |
| $29 / 40$ | 40 | $27: 9$ | $x^{2}-5 x-36$ |
| $y=-2$ | 11 | $8=3(2)-1$ <br> No | $128.6^{\circ}$ |

## Solving Linear Equations

## (with the unknown on both sides)

Solve the following equations:
(a) $5 x+8=4 x+11$
(b) $6 x+2=3 x+14$
(c) $x+4=3 x+1$
(d) $7 x-2=2 x+8$
(e) $5 x-2=9 x-2$
(f) $4 x+6=-3 x+20$
(g) $10-x=2 x-5$
(h) $4(2 x-7)=3(x-6)$

Watch this video to see how to do the examples. Remember to pause the video when promoted to copy the notes.

## Solving Linear Equations

## (with the unknown on both sides)

Solve the following equations:
(a) $\mid 5 x+8=\underline{4 x}+11$
$-4 x \mid$
$-8\left|\begin{array}{l}5 x+8-4 x=4 x+1-4 x \\ x+8=11 \\ x=3 \\ \text { Cnech } \\ 5(3)+8=4(3)+11\end{array}\right|-4 x$

$\left.\begin{aligned} & \text { (c) } \mid x+4=3 x+1 \\ &-x \\ &-1 \\ &-2=2 x+1 \\ & \div 2=2 x \\ & 3 / 2=x\end{aligned} \right\rvert\,-x$

- 'Solve' means
find the value of the letter
- start by subtracting the least anount


Chede $6(4)+2=3(4)+14 V$

(g) $10-x=2 x-5$

| $+x$ | $10=3 x-5$ | $+x$ |
| :--- | :---: | :---: |
| +5 | $15=3 x$ |  |
| $\div 3$ | $5=x$ | +5 |
|  | $\boxed{5}$ |  |


| $-3 x$ | $8 x-28=\underline{3 x}-18$ |
| :--- | :---: |
| +28 | $5 x-28=-18$ |
| $\div 5$ | $5 x=10$ |
| $x=2$ |  |$|+28$

- Reonember to

Check your
solution

substitution


## I'm giving it a try!

## Solve the following equations:

(1) $2 x=x+4$
(2) $3 x=2 x+4$
(3) $3 x+1=2 x+5$
(4) $3 x+2=2 x+6$
(5) $4 x+2=3 x+6$
(6) $3 x+6=4 x+2$
(7) $6 x+4=5 x+9$
(8) $9 a+8=10 a+5$
(9) $3 x=x+4$
(10) $4 x=2 x+4$
(11) $4 x+1=2 x+5$
(12) $4 x+2=2 x+6$
(13) $5 x+2=3 x+6$
(14) $3 x+6=5 x+2$
(15) $8 x+3=6 x+11$
(16) $5 w+18=7 w+4$
(17) $5 x+1=2 x+7$
(18) $4 x+5=7 x+2$
(19) $5 x+3=x+11$
(20) $3 x+38=8 x+8$
(21) $6 x+3=3 x+3$
(22) $12 t+1=8 t+3$
(23) $9 x+5=6 x+2$
(24) $9 x+4=11 x+10$

## Answers

## I'm giving it a try!

(1) $x=4$
(2) $x=4$
(3) $x=4$
(4) $x=4$
(5) $x=4$
(6) $x=4$
(7) $x=5$
(8) $a=3$
(9) $x=2$
(10) $x=2$
(11) $x=2$
(12) $x=2$
(13) $x=2$
(14) $x=2$
(15) $x=4$
(16) $w=7$
(17) $x=2$
(18) $x=1$
(19) $x=2$
(20) $x=6$
(21) $x=0$
(22) $t=0.5$ or $\frac{1}{2}$
(23) $x=-1$
(24) $x=-3$

## I'm building my confidence!

## Solve the following equations:

(1) $5 x-3=4 x+2$
(2) $8 x-1=6 x+5$
(3) $2 x+7=5 x-5$
(4) $x+1=3 x-1$
(5) $4 x-6=3 x$
(6) $7 x-6=4 x-3$
(7) $9 x-10=5 x-2$
(8) $6 x-5=4 x-9$
(9) $2 x-1=3 x-4$
(10) $4 x-20=10 x-2$
(11) $4 x+1=2 x-9$
(12) $3 x-6=7 x-4$
(13) $2 x+2=-x+11$
(14) $2 x+2=11-x$
(15) $-2 x+1=3 x+6$
(16) $5-3 x=7 x+20$
(17) $3 x-1=-x+7$
(18) $5-x=5 x-1$
(19) $-2 x+6=x-9$
(20) $3 x-2=1-3 x$
(21) $-x+1=-2 x+3$
(22) $7-7 x=12-2 x$
(23) $-2 x-10=5 x-10$
$(24)-1-2 x=5-10 x$

## Answers

## I'm building my confidence!

(1) $x=5$
(2) $x=3$
(3) $x=4$
(4) $x=1$
(5) $x=6$
(6) $x=1$
(7) $x=2$
(8) $x=-2$
(9) $x=3$
(10) $x=-3$
(11) $x=-5$
(12) $x=-0.5$ or $-\frac{1}{2}$
(13) $x=3$
(14) $x=3$
(15) $x=-1$
(16) $x=-1.5$ or $-1 \frac{1}{2}$
(17) $x=2$
(18) $x=1$
(19) $x=5$
(20) $x=0.5$ or $\frac{1}{2}$
(21) $x=2$
(22) $x=-1$
(23) $x=0$
(24) $x=0.75$ or $\frac{3}{4}$

## I'm ready for anything!

## Solve the following equations:

(1) $4 x=3(x+1)$
(2) $3(x+4)=2(x+9)$
(3) $5(x+2)=3(x+4)$
(4) $2(x+5)=6(x-1)$
(5) $4(x-5)=7(x-2)$
(6) $8(2 x-5)=3(5 x-10)$
(7) $5(2 x+5)=3(6 x+7)$
(8) $9(2 x-5)=3(4 x+7)$
(9) $2(2 x+4)=4(2-x)$
(10) $10(3 x-4)=20(5-2 x)$
(11) $6(3-4 x)+14=8(3 x+1)$
(12) $5(2-7 x)+25 x=2(6-4 x)$

## Answers

## I'm ready for anything!

(1) $x=3$
(2) $x=6$
(3) $x=1$
(4) $x=4$
(5) $x=-2$
(6) $x=10$
(7) $x=0.5$ or $\frac{1}{2}$
(8) $x=11$
(9) $x=0$
(10) $x=2$
(11) $x=0.5$ or $\frac{1}{2}$
(12) $x=-1$

## Extension

| By using your knowledge <br> about isosceles triangles, <br> find: <br> (a) the value for $\mathbf{x}$ <br> (b) the perimeter of the <br> triangle | By finding the value for $\mathbf{x}$ <br> first, find the value for $\mathbf{y}:$ | Explain why the following <br> equation has no solutions: |
| :--- | :---: | :---: |
|  | $6 x-3=2 x+29$ | $4(3 x+2)=12 x+5$ |

## Answers

By using your knowledge about isosceles triangles, find:
(a) the value for $x$
(b) the perimeter of the triangle

(a) $18-x=3 x+12$

$$
x=1.5
$$

(b) $18-x+3 x+12+4 x$

$$
\begin{aligned}
& =30+6 x \\
& =30+6(1.5)=39
\end{aligned}
$$

By finding the value for $x$ first, find the value for $y$ :

$$
6 x-3=2 x+29
$$

$$
5 x+17=4 x+2 y-3
$$

$$
\begin{gathered}
4 x-3=29 \\
4 x=32 \\
x=8
\end{gathered}
$$

$$
\begin{gathered}
5(8)+17=4(8)+2 y-3 \\
57=29+2 y \\
2 y=28 \\
y=14
\end{gathered}
$$

Explain why the following equation has no solutions:

$$
\begin{gathered}
4(3 x+2)=12 x+5 \\
12 x+8=12 x+5 \\
\text { now subtract } 12 x \\
8=5
\end{gathered}
$$

this does not make sense

| Retrieval Homework | Topic Homework |
| :--- | :--- |
| 1) Calculate $\frac{3}{8}+\frac{3}{7}$ | Solve the following equations: <br> (a) $6 x+3=5 x+5$ |
| 2) Share 162 in the ratio $3: 6$ | (b) $7 x+1=4 x+10$ |
| 3) Expand $(x-8)(x+4)$ | (c) $2 x+3=4 x+5$ |
| 4) Increase $£ 180$ by $83 \%$ | (d) $9 x-11=4 x+9$ |
| 5) Solve $9(4 y+1)=81$ | (e) $2 x+4=8 x+4$ |
|  | (f) $-x+2=5 x-1$ |
| (g) $2 x-4=8-2 x$ |  |
| (h) $2(x-3)=3(5 x+11)$ |  |

My Reflections..


## Answers

## Homework

## Retrieval Homework

(1) $\frac{45}{56}$ (2) $54: 108$ (3) $x^{2}-4 x-32$ (4) $£ 329.40$ (5) $\mathrm{y}=2$

Topic Homework
(a) $x=2$
(b) $x=3$
(c) $x=-1$
(d) $x=4$
(e) $x=0$
(f) $x=0.5$ or $\frac{1}{2}$
(g) $x=3$
(h) $x=-3$

